
Paths to synchronization

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Abstract

This work shows a new approach to the study of dynamic systems that act on a graph $\{G\} = (V, E)$ and that synchronize. As a first example, we take a simple linear system, known as the Laplacian associated with the adjacency matrix of $\{G\}$ the ODE on \mathbb{R}^V

$\frac{dx}{dt} = L_{\{G\}}(x)$, where $|V|=n$ and $L_{\{G\}}$ is the Laplacian matrix of the adjacency matrix of $\{G\}$. Which can also be written as: $\frac{dx_k}{dt} = \sum_{j \in V} A_{kj} x_j - d_k x_k$

Keywords: synchronization, Kuramoto model, Laplacian model, paths, graph theory

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